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11-4 Linear, Quadratic, and Exponential Models.....#

Objectives

Compare linear, quadratic, and exponential models.

Given a set of data, decide which type of function models the data and write an equation to describe the function.

Mar 14-11:19 AM

Feb 28-9:33 AM

Can you draw a picture of a(n)...

Linear Function

 Linear Equation Example:
 $y = mx + b$
 $y = \frac{1}{2}x + 5$

Quadratic Function

 Quadratic Equation Example:
 $y = x^2 + 4$

Exponential Function

 Exponential Equation Example:
 $y = 1(2)^x$
 $y = a(b)^x$

Feb 21-8:22 AM

Look at the tables and graphs below. The data show three ways you have learned that variable quantities can be related. The relationships shown are linear, quadratic, and exponential.

Linear

Age (yr)	Beats/min
20	170
30	161.5
40	153
50	144.5

Handwritten notes: $161.5 - 170 = -8.5$, $153 - 161.5 = -8.5$, $144.5 - 153 = -8.5$

Quadratic

Time (s)	Height (ft)
0.4	10.44
0.8	12.78
1	12
1.2	9.96

Handwritten notes: $12.78 - 10.44 = 2.32$, $12 - 12.78 = -0.76$, $9.96 - 12 = -2.04$

Exponential

Round	Teams Left
1	16
2	8
3	4
4	2

Handwritten notes: $16 \div 2 = 8$, $8 \div 2 = 4$, $4 \div 2 = 2$

Mar 14-11:22 AM

Write this in your notes!

Remember!

When the independent variable changes by a constant amount,

- linear functions have constant first differences.
- quadratic functions have constant second differences.
- exponential functions have a constant ratio.

Mar 14-12:13 PM

Graph each data set. Which kind of model best describes the data?

Time(h)	Bacteria
0	24
1	96
2	384
3	1536
4	6144

Plot the data points and connect them.

The data appear to be exponential.

Mar 14-11:27 AM

Graph each data set. Which kind of model best describes the data?

Boxes	Reams of paper
1	10
5	50
20	200
50	500

Handwritten notes: $\frac{rise}{run} = \frac{40}{8} = 5$, $\frac{150}{15} = 10$, $\frac{300}{30} = 10$

Plot the data points and connect them.

The data appears to be

Mar 14-11:27 AM

Graph each set of data. Which kind of model best describes the data?

x	y
-3	-14
-2	-9
-1	-6
0	-5
1	-6
2	-9
3	-14

Plot the data points.

The data appears to be quadratic.

Mar 14-11:54 AM

Look for a pattern in each data set to determine which kind of model best describes the data.

Money in CD	
Time (yr)	Amount (\$)
0	1000.00
1	1169.86
2	1368.67
3	1601.04

Handwritten notes: $\frac{1169.86}{1000} = 1.17$, $\frac{1368.67}{1169.86} = 1.17$, $\frac{1601.04}{1368.67} = 1.17$. For every constant change in time of +1 year there is an approximate constant ratio of 1.17.

The data appears to be exponential.

Mar 14-12:04 PM

Look for a pattern in the data set $\{(-2, 10), (-1, 1), (0, -2), (1, 1), (2, 10)\}$ to determine which kind of model best describes the data.

Write the information in a table...

Data (1)	Data (2)
-2	10
-1	1
0	-2
1	1
2	10

Handwritten notes: $10 - 9 = 1$, $1 - 3 = -2$, $-2 - 3 = -5$, $1 - 2 = -1$, $10 - 1 = 9$. $-3 + 9 = 6$, $3 - 3 = 0$, $9 - 3 = 6$.

The data appear to be quadratic.

Mar 14-12:08 PM

After deciding which model best fits the data, you can write a function. Recall the general forms of linear, quadratic, and exponential functions.

General Forms of Functions		
LINEAR	QUADRATIC	EXPONENTIAL
$y = mx + b$	$y = ax^2 + bx + c$	$y = ab^x$

Write a function to model each set of data.

1) Number of Computers

Year	1	2	3	4
Computers	14	28	56	112

Handwritten notes: $y = 14(2)^x$

2) Cost of Peaches

Pounds	1	2	3	4
Cost (\$)	1.29	2.58	3.87	5.16

Handwritten notes: $y = 1.29x$

3) Miles driven

Miles driven	5	6	7	8	9	10	11
Gallons of gas left in the tank	12	11.9	11.8	11.7	11.6	11.5	11.4

Mar 14-12:12 PM

Assignment: p.793(1-7, 14, 16-22, 27-29)

Mar 8-8:36 AM